

Lesson 7.5 – Properties of Linear Systems

Specific Outcome: 9.1 – Model a situation, using a system of linear equations. 9.6 – Explain, using examples, why a system of equations may have no solution, one solution or an infinite number of solutions.

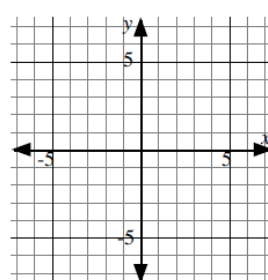
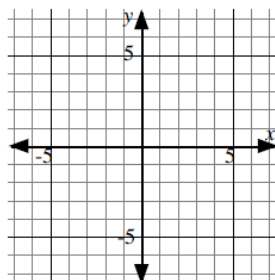
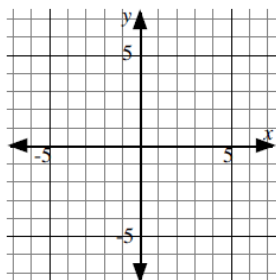
So far we have only worked with linear systems that have one solution (one point of intersection).

Work in groups of 2 or 3. Graph each of the following linear systems.

a) $-2x + y = 2$
 $2x + y = 2$

b) $-2x + y = 2$
 $-2x + y = 4$

c) $-2x + y = 2$
 $-4x + 2y = 4$



How many solutions does each linear system have?

Graphs of Lines	Slopes	Intercepts	Number of Solutions
Intersecting 	Different	Different	ONE
Parallel 	Same	Different	NONE
Coincident 	Same	Same	INFINITELY MANY

Practice:

1. Use the table to determine the number of solutions of each linear system.

a) $x + y = -2$
 $-2x - 2y = 4$

b) $4x + 6y = -10$
 $-2x - y = -1$

c) $3x + y = -1$
 $-6x - 2y = 12$

$$\begin{array}{l} \text{d) } x + y = 3 \\ \quad -2x - y = -2 \end{array}$$

e) $4x + 6y = -10$
 $-2x - 3y = 5$

f) $2x - 4y = -1$
 $3x - 6y = 2$

2. Given the equation $-2x + y = 4$, write another linear equation that will form a linear system with:
- a) exactly 1 solution b) no solution c) infinite solutions

Problem Solving: Determine how many solutions each linear system has.

1. Nadine has a cup of nickels and a cup of dimes. The total number of coins is 300 and their value is \$23.25. How many coins are in each cup?
2. Prana has a savings account and a chequing account with a total balance of \$85. His parents doubled the amount in each account and the new total balance is \$170. How much money does Prana have in each account?